

AM 9524B Computation of Dynamical Systems and Applications

(Winter 2016-2017)

- Time & Place: Thursday 1:30-4:30 pm, Room MC 15B. (First meeting: Jan. 5, 2017)
- Instructor: Pei Yu
- Office: MC 283, Ext: 88783, E-mail: pyu@uwo.ca

1. Course Outline

This course provides the students with a combination of symbolic and numerical computational methods for nonlinear systems, as well as applications to physical and biological problems. The nonlinear systems discussed in this course includes those described by *map*, *ordinary* differential equations and *partial* differential equations. Topics covered include stability and bifurcation, Hopf bifurcation, limit cycles, Bogdanov-Takens bifurcation and homoclinic/heteroclinic bifurcations, center manifold theory and normal form theory, perturbation methods and Melnikov's method.

- (1) Brief review of basic concepts in differential equations and dynamical systems.
- (2) Stability of equilibria: stability and asymptotic stability, classifications, nonlinear sinks, limit sets, Lyapunov's theorem, autonomous systems, gradient systems, Hamiltonian systems, and applications.
- (3) Periodic attractors: asymptotic stability of closed orbits, discrete dynamical systems, stability and closed orbits, Poincare maps, and applications.
- (4) Bifurcation theory, perturbation methods and Melnikov function method, Hopf bifurcation, Bogdanov-Takens bifurcation, homoclinic/heteroclinic bifurcation, center manifold and normal form theories.
- (5) Computation methods: symbolic computations for center manifolds and normal forms, limit cycles and Hilbert's 16th problem, numerical bifurcation method.
- (6) Applications of dynamical analysis to physical and biological problems, with demonstration of using software packages.

2. Text

None. Notes will be available in .pdf format. A list of the pertinent reference literature will be provided.

3. Course Evaluation

- (a) Assignments (once every two weeks): 40%
- (b) Project (presentation and report/paper): 60%